# **Non-Empirical LCAO-MO-SCF Calculations with Gaussian Type Functions on the Electrocyclic Transformation of Cyclopropyl to Allyl**

# **II. Anion Transformation**

## **D. T.** CLARK

Department of Chemistry, The University, Durham

## **D. R.** ARMSTRONG

Computing Laboratory, The University, Newcastle-upon-Tyne

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Non-empirical molecular quantum chemical calculations have been performed on the electrocyclic transformation of planar and non planar cyclopropyl anions, to allyl anions in the LCAO-MO-SCF framework using gaussian type functions as atomic orbitals. Employing a total of 37 GTF 3 disrotatory and 2 conrotatory modes of transformation have been considered. A total of 34 calculations have been carried out. In the transformation of planar and non planar cyclopropyl anions to allyl anions, both the disrotatory and conrotatory modes possess activations barriers, those for the conrotatory modes being the lower by substantial margins. A detailed analysis of the energy terms involved show that is little theoretical justification for the postulate that the mode of ring opening depends only on the symmetries of the highest occupied orbitals.

Nichtempirische SCF-MO-Rechnungen mit Gaußfunktionen (GF) für den Übergang des planaren und des unplanaren Cyclopropylanions zum Allyanion wurden vorgenommen. Mit einem Basissatz von 37 GF wurden 34 Rechnungen für 3 disrotatorische und 2 conrotatorische Übergänge durchgeführt. Sowohl die disrotatorischen als auch die conrotatorischen Übergänge besitzen Aktivierungsbarrieren, von denen diejenigen für die conrotatorischen Übergänge stets kleiner sind. Die Analyse der Energieterme gibt wenig Anlal3 zu der Annahme, dab die Art der Ring6ffnung nur von der Symmetrie des obersten besetzten Orbitals abhängt.

Des calculs *ab-initio* en orbitales gaussiennes ont été effetués sur la transformation de cations cyclopropyliques en cations allyliques. Les barrières d'activation sont toujours plus basses pour la mode conrotatoire que pour la mode disrotatoire. Il est peu evident que l'ouverture du cycle dépende que de la symmetrie de la plus haute orbitale occupée.

#### **1. Introduction**

In Part I [1] we presented the results of an *ab initio* treatment of the transformations of cyclopropyl to allyl cation. In this paper we present similar results for the anion transformations.

In a previous communication  $\lceil 2 \rceil$  the ground state and lower excited singlet and triplet state energy differences between various modes of transformation of cyclopropyl to allyl anion have been investigated by a semi empirical all valence

SCF MO method. The motivation for this investigation was to clarify the original predictions of Woodward and Hoffmann [10] and Longuet-Higgins and Abrahamsom [8] particularly for transformations involving excited states. However, although the semi empirical all valence SCF MO treatment is on a surer theoretical basis for charged species, than EHT used in the original work, the method is unsatisfactory [2, 3] for calculating energy changes between species in which the bond lengths are different. On the other hand an *ab initio* treatment has the principal disadvantages of requiring relatively powerful computing facilities but has the major advantage that all the terms of the total energy are effectively calculated and that one can then distinguish the contribution of each of them to a global energetic effect. This allows a detailed comparison of energy differences between various modes of transformation to test the validity of the Woodward Hoffmann approach.

As in the previous work [1] the transformations of both planar and non planar cyclopropyl species have been-investigated, the definition of the various modes being as described previously. However the emphasis of the work is slightly changed from that of the cationic species since calculations show that a free cyclopropyl anion is non planar anyway so that the  $Dis(1)$ ,  $Dis(2)$  and  $Con(1)$ modes of transformations [1, 3] are prototypes for both the *concerted* and *non concerted* transformation of cyclopropyl to allyl anion. The Dis(0) and Con(0) [1, 3] modes then represent hypothetical transformations of a planar cyclopropyl anion to allyl anion. However this also has considerable interest since one of the most unsual findings in the cationic case [1] was that in the disrotatory transformation of *planar* cyclopropyl cation after  $\sim 30^\circ$  angle of rotation on the reaction co-ordinate the *non planar* species corresponding to the Dis(2) mode became the more favoured. It is of interest therefore to see if this behaviour is mirrored in the case of a non planar cyclopropyl anion where perhaps the planar species might become the favoured one as the transformation proceeds.

# **2. Method of Calculation**

The calculations performed in this work were carried out using the Polyatom system [4, 5] tailored to make use of the extensive disc handling facilities of the NUMAC IBM 360/67. The five modes of transformation were studied at  $15^\circ$ intervals in the rotation of the  $H2-C2-H3$  (H4–C3–H5) planes with respect to the plane of the ring. The numbering system co-ordinate axes, bond angles and bond lengths used in the calculations were as previously given [1, 3]. The integrals generated for each point on the reaction co-ordinate, for the cationic species were stored on disc (IBM 2314) and were then utilized in the SCF procedure for both the cation and anion. In particular cases however difficulty was experienced with convergence of the SCF procedure, and despite using several devices which we have previously found to be useful in such cases, convergent solutions were not obtained for the points corresponding to  $Dis(1)$  and  $Con(1)$  $45^\circ$ . However for a  $50^\circ$  angle of rotation the solutions were convergent. A total of 34 calculations have been carried out, a basis set of 37 GTF being used as previously described.

#### **3. Results and Discussion**

## *3.1. Energies for Bent and Planar Cyclopropyl and Allyl anions*

Table 1 shows the energies and symmetries of the occupied and two lowest energy virtual orbitals for bent and planar cyclopropyl and allyl anions. The energy of each orbital is considerably higher than the corresponding orbital of the cation [1], in particular the effect of the extra two electrons on the carbon ls orbitals should be noted. For the planar cyclopropyl anion the highest occuped and lowest energy virtual orbitals are of "pseudo"  $\pi$ -symmetry, consisting of the carbon  $p_r$  orbitals and anti-symmetric combinations of the hydrogen 1s orbitals. The occupied orbital is concentrated about C1 whereas the virtual

	Cyclopropyl anion		Allyl anion	
	Bent	Planar		
Virtual orbitals	$+0.6003 A'' 14\sigma^*$	$+0.6002 B2 14\sigma^*$	$+0.5507$ A1 14 $\sigma^*$	
	$+0.5272 A' 13\sigma^*$	$+0.5584 B1 13\sigma^*$	$+0.4694 B1 13\pi*$	
Occupied orbitals	$+0.0104 A' 12\sigma$	$+0.0357 B1 12\sigma$	$+0.0231$ A2 $12\pi$	
	$-0.1439 A'' 11\sigma$	$-0.1351 B2 11\sigma$	$-0.1698 B1 11\pi$	
	$-0.1879 A' 10\sigma$	$-0.1933 A1 10\sigma$	$-0.2486 B2 10\sigma$	
	$-0.2781 A''$ $9\sigma$	$-0.2684$ A2 $9\sigma$	$-0.2538$ A1 $9\sigma$	
	$-0.3360 A' 8\sigma$	$-0.3589$ A1 $8\sigma$	$-0.3140 B2$ $8\sigma$	
	$-0.4157 A'$ $7\sigma$	$-0.4008$ B1 $7\sigma$	$-0.3768$ A <sub>1</sub> $7\sigma$	
	$-0.5067 A'$ 6σ	$-0.4879$ A1 6σ	$-0.4966 A1$ 6σ	
	$-0.5727 A''$ $5\sigma$	$-0.5650 B2$ $5\sigma$	$-0.6218 B2$ $5\sigma$	
	$-0.8656 A'$ $4\sigma$	$-0.8494 A1$ 4σ	$-0.7672$ A1 $4\sigma$	
	$-10.5179 A'$ $3\sigma$	$-10.5131$ A1 $3\sigma$	$-10.5471$ A1 $3\sigma$	
	$-10.6360 A''$ $2\sigma$	$-10.6354 B2$ $2\sigma$	$-10.5472 B2$ $2\sigma$	
	$-10.6358 A'$ $1\sigma$	$-10.6362$ A <sub>1</sub> $1\sigma$	$-10.6289$ A1 $1\sigma$	
Electronic energy	$-180.26367$	$-179.86996$	$-176.18932$	
Nuclear energy	68.42081	68.02974	64.24261	
Total energy	$-111.84286$	$-111.84022$	$-111.94671$	

Table 1. *Energies and symmetries of the occupied and two lowest energy virtual orbitals for bent-and planar cyclopropyl and allyl anions (energies in a. u.)* 

orbital is spread over  $C2$ ,  $C3$  and the hydrogen atoms. In allyl anion the corresponding orbitals are of  $\pi$ -symmetry the highest occupied orbital consisting of an anti symmetric combination of C2 and C3  $p_x$  orbitals, whilst the lowest virtual orbital is concentrated largely on C 1. Applying Koopman's theorem the ionisation potential of the anions, equal to the negative of the electron affinity of the corresponding radicals are calulated to be 0.971 eV, 0.283 eV and 0.629 eV for planar, non planar cyclopropyl and allyl respectively. These values would appear to be reasonable (cf.  $CH_3$  1.08 eV [9]).

The calculations indicate that a free cyclopropyl anion will adopt a "bent" configuration about  $C_1$ , the difference in energy between the bent and planar configurations being 1.66kals/mole. The nuclear energy favours the planar form by a considerable margin but this is just offset by the lower electronic energy of the non planar form.

For the transformation of non planar cyclopropyl to allyl anion the calculated energy change is 0.1039 a. u. (65.2 kals/mole). This is almost indentical to the value obtained for the cation transformation with the same size basis set [1].

# *3.2. Analysis of Energy Terms for the Disrotatory and Conrotatory Modes of Transformation for a Bent Cyclopropyl Anion, Analogue for a Concerted and Non Concerted Reaction Process*

As we have already indicated the situation involving the anion is somewhat different from that of the cation where the free cyclopropyl species adopted a planar configuration about  $C1$  [1]. For the anion the non planar configuration of cyclopropyl is energetically preferred so that the  $Dis(1)$ ,  $Dis(2)$  and  $Con(1)$ modes serve as models for both the concerted and non concerted processes.



Fig. 1. Energy (a. u.) versus angle of rotation  $\degree$  for Dis(1), Dis(2) and Con(1) transformation of cyclopropyl to allyl anion

Fig. 1 shows a plot of energy versus reaction co-ordinate for the three modes. An interesting feature here is that in contrast to the cation case where the favoured Dis(0) mode showed no activation barrier, all three modes of transformation possess activation barriers of 73.95 kals/mole, 73.95 kals/mole and 26.92 kals/mole for the  $Dis(1)$ ,  $Dis(2)$  and  $Con(1)$  modes respectively. For the non concerted reaction therefore in which an initially formed cyclopropyl carbanion is produced which then rearranges, one would expect the anion to have a substantial lifetime, this is in contrast to the cation which has a great propensity ro rearrange since the Dis (0) modes requires no activation barrier. The conrotatory mode is clearly favoured as predicted by EHT in the original work [10] and confirmed by the all valence electron SCF MO calculations [2]. Since the effect of the leaving group is not specifically taken into account for the concerted reaction we cannot say anything about the activation barriers for this type of process, however the *energy differences* between the modes should be mirrored in the non concerted

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transformation of the non planar cyclopropyl anion so that again the conrotatory process should be clearly favoured. There appears to be no experimental evidence as yet for the ring opening of cyclopropyl anion itself, however a derivative of the isoelectronic aziridine ring system has been studied. Huisgen and co-workers [6] have studied the thermolysis of both cis and trans dimethyl 1 (4 methoxy phenyl) aziridine 2,3 dicarboxylate and by trapping the intermediate ring opened azomethine ylids with dimethyl acetylene dicarboxylate have shown that ring opening occurs stereospecifically in a conrotatory fashion.

Fig. 2 shows a plot of the orbital energies for both the occupied and two lowest energy virtual orbitals for the  $Dis(1)$ ,  $Dis(2)$  and  $Con(1)$  modes of transformation. For the disrotatory modes the highest occupied orbital of bent cyclopropyl anion correlates with the lowest virtual orbital of allyl anion. As in the cation case [1] there are significant changes in the inner shell carbon Is orbital energies.

The various energy terms contributing to the total energy may be written as follows Eq.  $(1)$ .

$$
E_{\text{Total}} = E_1 + E_2 + E_3 \tag{1}
$$

where  $E_1 = \text{sum of orbital energies},$  $E_2$  = sum of electron repulsion terms,  $E_3$  = nuclear repulsion term.

Table 2 gives an analysis of these energy terms for the Dis(l), Dis(2) and Con(l) modes and also the energy differences between the modes. Also included are the contributions to the orbital energy term arising from the highest occupied orbitals, since according to Woodward and Hofmann [10] it is the energy differences arising in these orbitals that largely determines the energy difference between disrotatory and conrotatory modes. Considering first the energy terms for the Dis(l) and Con(l) modes, the major energy differences between these modes occurs in the region corresponding to  $30^{\circ} - 60^{\circ}$  angle of rotation along the reaction co-ordinate.

In each of the cases corresponding to 30 $^{\circ}$ , 50 $^{\circ}$ , and 60 $^{\circ}$  angles of rotation the lower energy of the  $Con(1)$  mode results largely from the lower electronic energy, the nuclear energy terms being much smaller and favouring the Con(1) mode. For a 30 $^{\circ}$  angle of rotation the lower electronic energy of the Con $(1)$  mode is attributed to the lower electron repulsion energy term, the orbital energy term actually favouring the disrotatory mode even though the contribution to the latter term arising from the highest occupied orbital is opposite in sign. At 50 $\degree$  and 60 $\degree$  the lower energy of the Con(1) mode is largely due to the lower orbital energy term the electron repulsion terms in each case strongly favouring the Dis(1) mode. However the contribution to  $\Delta E_1$  arising from the highest occupied orbital is by no means predominant. In fact there is very little correlation between  $\Delta E_1$  and the particular term in this summation arising from the highest occupied orbital as suggested by Woodward and Hoffmann [10]. The largest energy differences between the  $Dis(2)$  and  $Con(1)$  modes also occur in the region  $30^{\circ}$  -60 $^{\circ}$ , in this case however the nuclear energy terms are substantially larger and in each case favour the Con(1) mode. At 30 $\degree$  the lower energy of the Con(1)



mode arises mainly from  $\Delta E_1$  the orbital energy term, however for 50° and 60° angles of rotation the orbital energy and electron repulsion terms are of comparable magnitude, the preference for the  $Con(1)$  mode arising from a combination of nuclear and electronic energies. For a  $75^{\circ}$  angle of rotation however the electronic energy term actually favours the Dis(2) mode and the small preference for the  $Con(1)$  mode then arises from the nuclear energy term. It is clear however that 26\*



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as for the Dis(1) mode there is little correlation between the  $\Delta E_1$  terms and the individual terms arising from the highest occupied orbitals, indicating the gross oversimplification of Woodward and Hoffmann's arguments [10] for the cyclopropyl-allyl anion transformation.

# *3.3. Disrotatory and Conrotatory Transformation of an Initially Planar Cyclopropyl Anion*

As we have indicated a free cyclopropyl anion adopts a non planar configuration so that the transformation involving a planar species are to some extent academic. However there are two points of interest. Firstly do the energy curves for the preferred conrotatory modes, Con (1) and Con (0), involving the non planar and planar species respectively, cross over as the corresponding disrotatory modes do for the cation? Secondly for the planar species the two disrotatory modes Dis (1) and Dis (2) become identical, Dis (0) and it is of interest to compare



Fig. 3. Energy (a. u.) versus angle of rotation  $\circ$  for Dis(0) and Con(0) transformation of planar cyclopropyl to allyl anion

the energy difference between a conrotatory and disrotatory process as we have done for the cationic species.

Fig. 3 shows a plot of the energy of transformation against the reaction coordinates for the two modes of transformation. Both modes show activation barriers of 18.82 kals/mole and 70.90 kals/mole respectively for the Con(0) and Dis (0) modes. The activation energy difference 52.08 kals/mole may be compared with 46.2 kals/mole obtained [1] for the transformation involving the planar cations, the  $Con(0)$  mode being favoured for the anion and  $Dis(0)$  mode for the cation.

Table 3 shows an analysis of the energy terms for the  $Con(1)$  and  $Con(0)$ modes. The surprising feature here is that the planar species is actually the more stable for angles of rotation greater than  $15^{\circ}$  and this results from a lower nuclear energy, the electronic energy terms favouring the non planar species. Hence the transformation of a free cyclopropyl anion to allyl anion involves an initially



Table 3. *Detailed comparison of energy terms for the* Con(l) *and* Con(0) *modes (all energies in a. u.)*  Table 3. Detailed comparison of energy terms for the  $Con(1)$  and  $Con(0)$  modes (all energies in a. u.) non planar species which rapidly assumes a planar configuration about C 1 as the reaction proceeds in a conrotatory fashion. This is exactly the opposite behaviour to that exhibited by the cation [1].

#### *3.4. Electronic Distributions*

The gross atomic and bond overlap populations of the cyclopropyl and allyl anions are presented in Table 4, For all three anions the negative charge is spread over all the atoms. As might be expected there is a close similarity in electron distribution between the two cyclopropyl anions, except for the occupancy of the C 1  $p_x$  and H 1 orbitals. The charge distribution in allyl anion is somewhat similar to that of the cyclopropyl anions and this is in marked contrast to the

Electron densities	Planar cyclopropyl anion	Bent cyclopropyl anion	Allyl anion
C <sub>1</sub> S	2.538	2.620	2.642
$P_x$	1.827	1.569	$0.904 (\pi)$
$P_{y}$	0.944	0.904	1.319
$P_z$	1.106	1.088	1.208
Total	6.415	6.181	6.073
$C2, C3$ S	2.602	2.618	2.576
$P_{x}$	1.126	1.137	1.548 $(\pi)$
$P_{y}$	1.073	1.095	1.071
$P_z$	1.324	1.360	1.074
Total	6.125	6.210	6.269
H1	1.099	1.211	1.026
H2, H4	1.059	1.034	1.106
H3, H5	1.059	1.062	1.075
Bond populations			
$C1-C2$	0.700	0.693	0.839
$C2-C3$	0.475	0.504	$-0.053$
$C1-H1$	0.717	0.661	0.747
$C2-H2$	0.719	0.751	0.753
$C2-H3$	0.719	0.706	0.743

Table 4. *Electron densities and bond populations of bent and planar cyclopropyl and a!lyl anions* 

cation case [1]. The explanation for this equalization of charge is evident from the form of the highest occupied orbitals which produce a localisation of electrons in the C1  $p_x$  orbitals and in the C2, C3  $p_x$  orbitals for the cyclopropyl and allyl anions respectively (i. e. on those atoms in the corresponding cation which were positively charged).

The difference between allyl and cyclopropyl anions however is manifest in the C2-C3 bond overlap populations, the latter being strongly bonding for the cyclopropyl anions and slightly antibonding for the allyl anion. The changes in C2–C3 bond overlap populations for the  $Dis(0)$ , Con(0) and  $Dis(1)$ ,  $Dis(2)$ and Con(l) modes are illustrated in Figs. 4 and 5 respectively. Considering firstly the Dis(0) and Con(0) modes, for angles of rotation  $> 50^{\circ}$  the bond overlap populations are both negative, that for the Dis(0) mode being the larger, whilst



Fig. 4. Bond overlap populations between atoms C 2-C 3 for Dis (0) and Con (0) modes of transformation of planar cyclopropyl to allyl anion

for angles of rotation  $\langle 50^\circ \rangle$  the bond overlap populations are positive, again that for the Dis(0) mode being the larger. Comparing this with the energy plot Fig. 3 shows quite clearly that for a  $45^\circ$  angle of rotation where the energy gap between the Dis(0) and Con(0) modes is the largest the Dis(0) mode in fact has the larger C2-C3 bond overlap population, again pointing to the inadequacy of the simple Woodward-Hoffmann pictorial treatment [10]. In the case of the  $Dis(1)$ ,  $Dis(2)$  and  $Con(1)$  modes however, the situation is somewhat better. Comparison of the energy curves Fig. 1 and Fig. 5 the  $C2-C3$  bond overlap populations for the three modes shows some correlation between the two. Thus the antibonding situation develops more rapidly for the Dis(2) mode



Fig. 5. Bond overlap populations between atoms C2-C3 for Dis(l), Dis(2) and Con(l) modes of transformation of cyclopropyl to allyl anion

with respect to the Dis(1) mode and the major energy difference between the corresponding modes and the Con(l) mode also develops in the same way.

In the case of the cation a simple pictorial explanation has been advanced [7] for the lower energy of the Dis(2) mode with respect to the Dis(1) mode, a concerted reaction in terms of a favourable bonding interaction between orbitals on  $C_2$  and  $C_3$  and the vacant orbital of the developing carbonium ion at  $C_1$ . Our calculations [1] gave some support to this hypothesis, and indicated that for angles of rotation  $\langle 45^\circ \rangle$  where the energy difference between the two disrotatory modes was largest, there was a significant difference in the  $C1-C2(C3)$ bond overlap populations as required by the simple model. In the case of the



Fig. 6. Bond overlap populations between atoms C 1-C2 (C3) for Dis(l), Dis(2) and Con(l) modes of transformation of cyclopropyl to allyl anion

anion however one might expect this argument to be set in reverse i. e. the interaction between orbitals located at C2 and C3 with the doubly occupied orbital of the developing carbanion at C 1 should be unfavourable and again show up as a difference in C1–C2 (C3) bond overlap populations. For angles of rotation less than  $\sim 40^{\circ}$  (see Fig. 1) the Dis(1) mode is of considerably lower energy than the Dis(2) mode. Fig. 6 shows the C1–C2 (C3) bond overlap populations and again there is some evidence for the pictorial explanation since the major difference in  $C1-C2$  (C3) bond overlap population between the Dis $(1)$  and Dis $(2)$  modes occurs in the same region.

#### *3.5. Bond Length Variation in Allyl Anion*

The molecular geometries used are those previously described for the cation transformation [1, 3]. However as a check we have carried out calculations on allyl anion varying the C-C bond length with the C-H bond length fixed at 1.08 A. This shows a calculated minimum at 1.38 A, and this is almost identical

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to that obtained for the cation  $(1.37 \text{ Å})$ . This would indicate that the assumed initial and final geometries are reasonable.

By fitting a parabola to the potential energy curve a force constant for the symmetric stretching vibration of the C-C bonds of 13.47 mdyne  $A^{-1}$  was obtained.

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Dr. D. T. Clark Department of Chemistry The University Durham, England